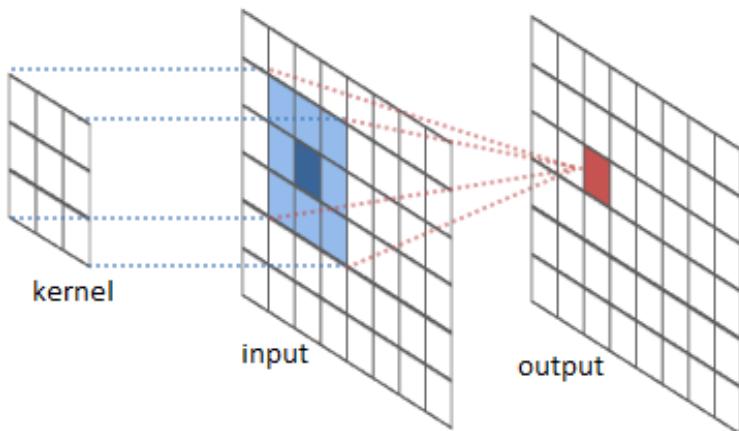


HW2 Sparse Matrices Convolution



$$\begin{bmatrix} 0 & 0 & 0 & 0 & 9 & 0 \\ 0 & 8 & 0 & 0 & 0 & 0 \\ 4 & 0 & 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 5 \\ 0 & 0 & 2 & 0 & 0 & 0 \end{bmatrix}$$

Rows	Columns	Values
5	6	6
0	4	9
1	1	8
2	0	4
2	2	2
3	5	5
4	2	2

Image Convolution

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} * \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

$$= (i * 1) + (h * 2) + (g * 3) + (f * 4) + (e * 5) + (d * 6) + (c * 7) + (b * 8) + (a * 9)$$

Image Convolution

- Using zero padding.

$$15*2 + 0*0 + 0*0 + 0*0 + 0*1 + 0*0 + 0*3 + 0*0 + 0*1 = 30$$

0	0	0				
0	0	0	0	0	0	0
0	0	15	0	0	22	0
0	0	11	3	0	0	0
0	0	0	0	-6	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

Image matrix

2	0	0
0	1	0
3	0	1

Filter matrix

30				

Output matrix

Image Convolution

- Using zero padding.

$$0*2 + 15*0 + 0*0 + 0*0 + 0*1 + 0*0 + 0*3 + 0*0 + 0*1 = 0$$

0	0	0				
0	0	0	0	0	0	
0	15	0	0	22	0	
0	0	11	3	0	0	
0	0	0	0	-6	0	
0	0	0	0	0	0	
0	0	0	0	0	0	

Image matrix

2	0	0
0	1	0
3	0	1

Filter matrix

30	0					

Output matrix

Image Convolution

- Using zero padding.

	0	0	0	0	0	0
0	0	0	0	0	0	0
0	15	0	0	22	0	0
0	0	11	3	0	0	0
0	0	0	0	-6	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

Image matrix

30	0	0				

Output matrix

2	0	0
0	1	0
3	0	1

Filter matrix

Image Convolution

- Using zero padding.

0	0	0	0	0	0
0	15	0	0	22	0
0	0	11	3	0	0
0	0	0	0	-6	0
0	0	0	0	0	0
0	0	0	0	0	0

Image matrix

30	0	0	44	

Output matrix

2	0	0
0	1	0
3	0	1

Filter matrix

Image Convolution

- Using zero padding.

0	0	0	0	0	0
0	15	0	0	22	0
0	0	11	3	0	0
0	0	0	0	-6	0
0	0	0	0	0	0
0	0	0	0	0	0

Image matrix

30	0	0	44	0	0
0	37	6	0	22	0
45	0	26	57	0	22
0	33	9	?		

Output matrix

2	0	0
0	1	0
3	0	1

Filter matrix

Image Convolution

- Using zero padding.

0	0	0	0	0	0
0	15	0	0	22	0
0	0	11	3	0	0
0	0	0	0	-6	0
0	0	0	0	0	0
0	0	0	0	0	0

Image matrix

30	0	0	44	0	0
0	37	6	0	22	0
45	0	26	57	0	22
0	33	9	11	-3	0
0	0	0	-18	0	-6
0	0	0	0	0	0

Output matrix

2	0	0
0	1	0
3	0	1

Filter matrix

Sparse Matrices

- Details are described in CH2 Array on iLMS.

	row	col	value
smArray[0]	0	0	15
[1]	0	3	22
[2]	0	5	15
[3]	1	1	11
[4]	1	2	3
[5]	2	3	6
[6]	4	0	91
[7]	5	2	28

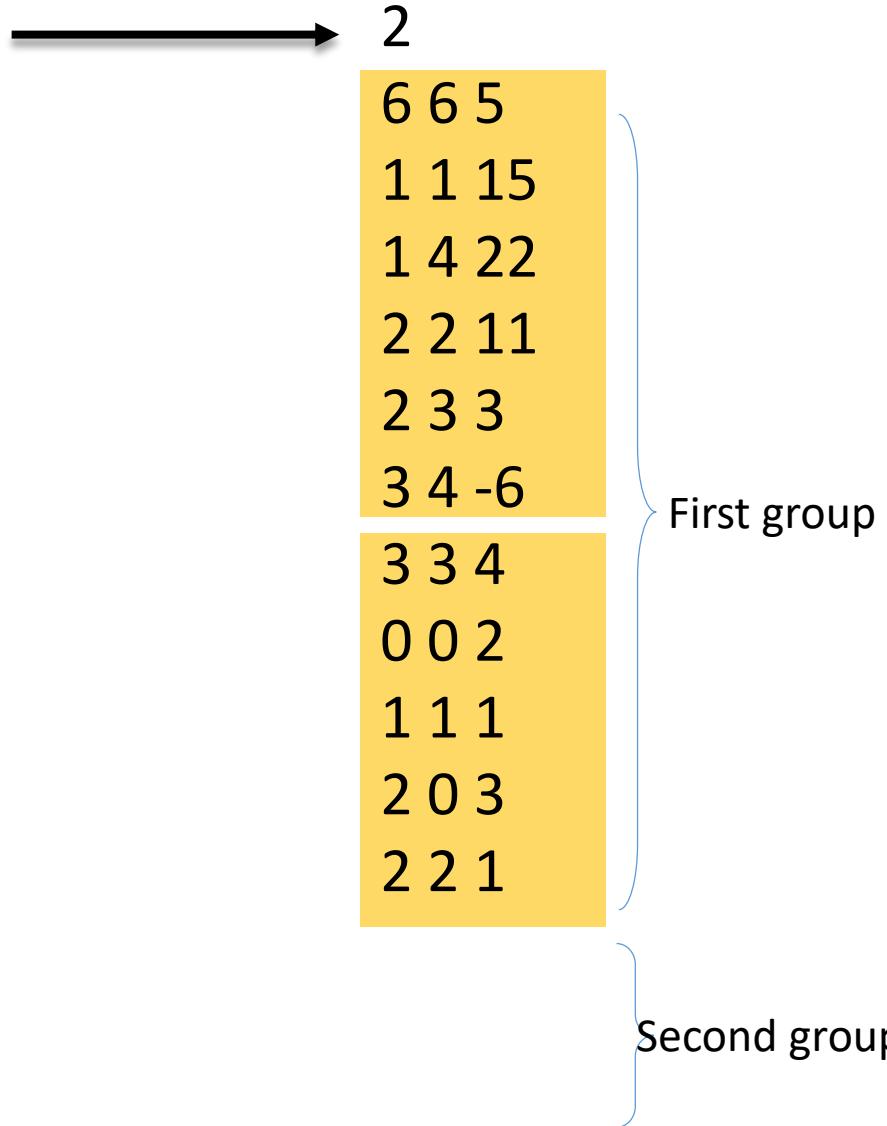
Eight non-zeros

$$\begin{bmatrix} 15 & 0 & 0 & 22 & 0 & 15 \\ 0 & 11 & \textcolor{red}{3} & 0 & 0 & 0 \\ 0 & 0 & 0 & 6 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 91 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 28 & 0 & 0 & 0 \end{bmatrix}$$

row { } col { }

Input

The first number describes the amount of matrix convolution we want to compute.



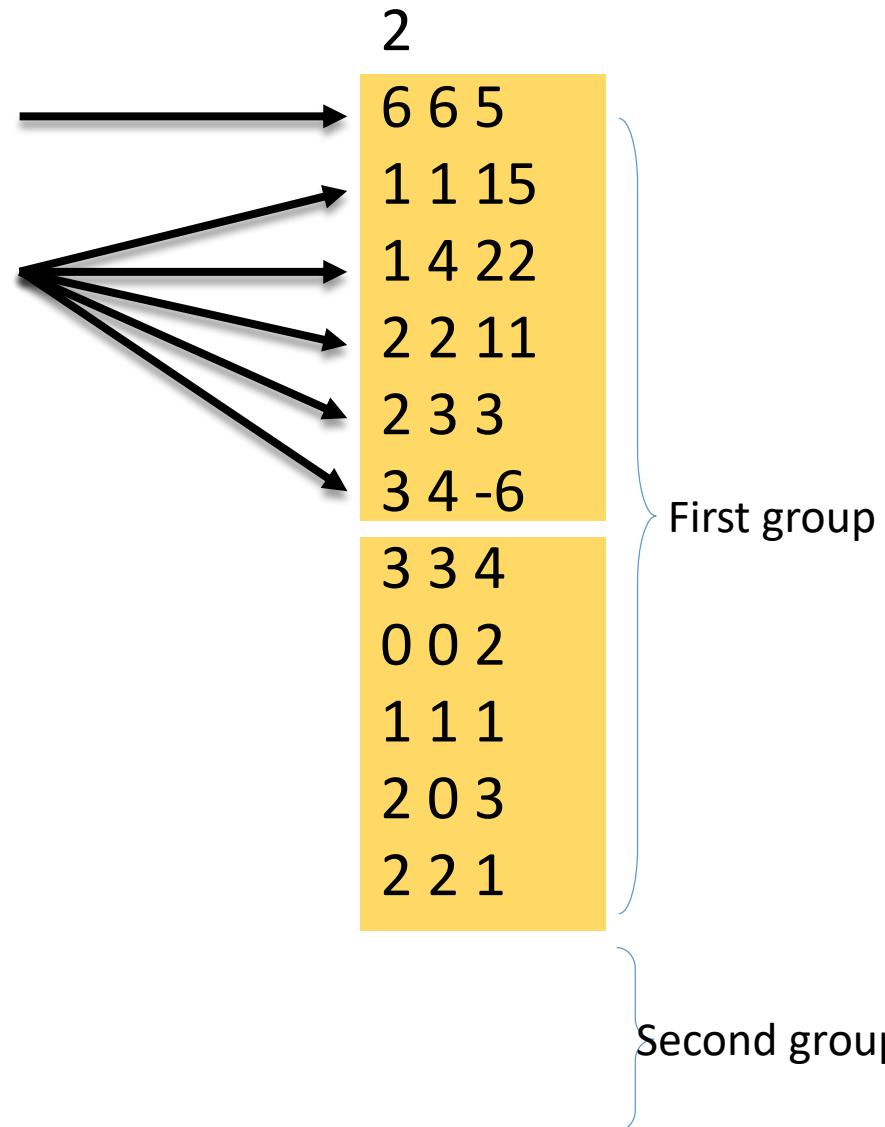
Input

Image matrix's #row, #col, #non-zeros.

Image matrix's non-zero term's row, col, value.

Example image matrix

0	0	0	0	0	0
0	15	0	0	22	0
0	0	11	3	0	0
0	0	0	0	-6	0
0	0	0	0	0	0
0	0	0	0	0	0



Input

Example filter matrix

2	0	0
0	1	0
3	0	1

Filter matrix's #row, #col, #non-zeros.

Filter matrix's non-zero term's row, col, value

2

6 6 5

1 1 15

1 4 22

2 2 11

2 3 3

3 4 -6

3 3 4

0 0 2

1 1 1

2 0 3

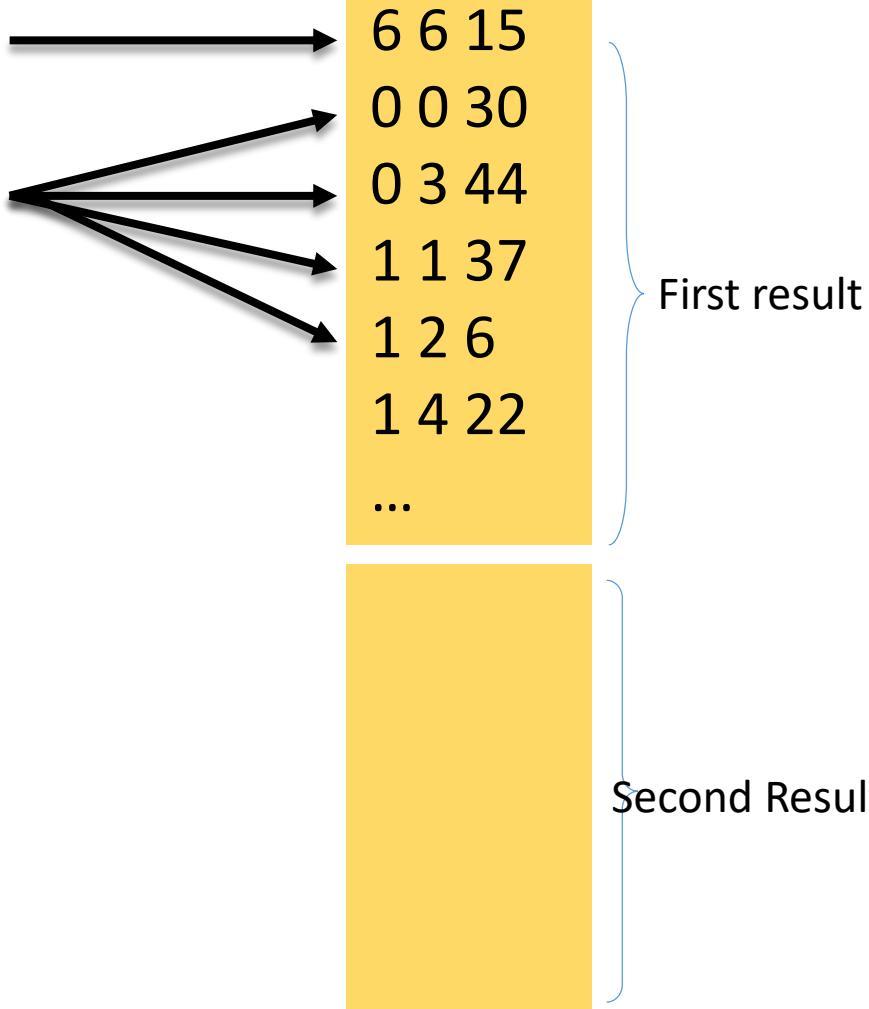
2 2 1

First group

Second group

Output

Output matrix's #row, #col, #non-zeros.



Example output matrix

30	0	0	44	0	0
0	37	6	0	22	0
45	0	26	57	0	22
0	33	9	11	-3	0
0	0	0	-18	0	-6
0	0	0	0	0	0